USING FUZZY LOGIC TO TUNE OPTIMIZATION PARAMETERS IN NEURAL MODEL BASED PREDICTIVE CONTROL TECHNIQUE

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ABSTRACT
The underlying idea of Model Based Predictive control can be summarized as follows: A plant model is used in order to predict its future behavior. Thus, Neural Networks (NN) are used in this work to build the target plant dynamic model. The control signal is calculated by means of an optimization problem, solved at each sampling period. Selecting "good" optimization parameters ("weights") is a very important issue. However, it is not easy to select these parameters so that some optimization requirements are achieved. In this work, we propose an algorithm for weights fuzzy self-tuning. Optimization requirements are translated in terms of fuzzy rules. As an application, this design technique was applied to solve the perturbation rejection problem for a multivariable benchmark “Continuous Stirred Tank Reactor” (CSTR).

KEYWORDS. Non-Linear Systems and Modeling, Process Control.

INTRODUCTION
Model Based Predictive Control (MBPC) is a well-known technique [1] that employs a model of the plant in order to predict its future behavior. In this approach, the control signal is calculated by means of an optimization problem, solved at each sampling period. The high computational complexity has restricted the use of this technology to relatively slow systems encountered in the chemical industry [2]. In other hand, Neural Networks (NN) have been used successfully in order to model and control complex nonlinear plant [3-4]. In this work, NN are used to "learn" the nonlinear dynamics of the target plant: a multivariable benchmark “Continuous Stirred Tank Reactor” (CSTR). This

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model is based on a recurrent Elman type NN, which acts as a nonlinear "universal approximator".

Whoever has worked with MBPC knows that selecting "good" weights is a crucial issue to solve the optimization problem. Yet, it is not easy to select these weights so that some optimization requirements (for instance, balanced optimization terms) are achieved. In general, there exist some "rules of thumb" that allow selecting it heuristically, by "trial and error" procedures based on simulations results. In this way, finding a good parameters set can be long and annoying. In this work, we propose a weight self-tuning procedure using a Fuzzy Inference System (FIS). This kind of intelligent systems has been used to help making decisions in many engineering fields. The self-tuning procedure is run "on-line" during a training period before starting the MBPC optimization at each sampling period. Optimization requirements are translated in terms of fuzzy rules, whose input variables are the same as the optimization problem.

The following exposition is organized as follows. First, a process description is given. Then, the controller design method is described in detail. Simulations results are given to show the controller ability to reject perturbations. Finally some conclusions are presented.

PROCESS DESCRIPTION

The controlled process, depicted in Fig. 1, consists on a benchmark CSTR, which is a multivariable highly coupled and nonlinear chemical plant. It has been described in [5] and is adopted unchanged in this paper. Within the tank, it is assumed that the liquid can be considered homogeneous. The reaction takes place at the temperature value T and concentration values Ca and Cb. The molar input flow of product A, labeled F, has a concentration Ca0 and its temperature is T0. The heat Qk is removed by means of a cooling jacket. Energy and matter balance may be set for the whole reactor volume.

CONTROLLER DESIGN METHOD.

The control scheme is shown in Fig.2. The controlled process has two inputs (F and Qk) and two outputs (Cb and T). The proposed controller consists mainly of three different sub-systems:

1. A “Neuronal Model”.
3. A Fuzzy “Weight Tuner”.

Each controller block is described in following sections.
The neuronal model.

The recurrent Elman type NN structure is shown in Fig.3. It was adapted from [6]. It is a simple not coupled structure because there is not interaction between units of hidden layer belonging to different outputs. Each hidden layer has 10 units. When this number was increased the quality of the model did not improve. A tangential function was used in the hidden layer and a linear function in the output layer. In order to train the net, several simulations were carried out, letting some perturbations act on the process.
The control goal was rejecting perturbations in variable $T_0$. An integral action was included in the process (which does not have one itself) in order to reduce steady state offsets. The NN was trained taking into account this integral action. Simulations were carried and data was collected using a *Simulink* block model. Training was done off-line using *MATLAB NN Toolbox*.

The NN model equations are:

$$
\begin{align*}
  y_1(t) &= T(t) \\  y_{r1}(t) &= y_1 \\  u_1(t) &= F(t) \\  \dot{y}_1(t+1) &= N_1(X(t)) \\
  y_2(t) &= Ch(t) \\  y_{r2}(t) &= y_2 \\  u_2(t) &= Q_k(t) \\  \dot{y}_2(t+1) &= N_2(X(t))
\end{align*}
$$

**Optimizer**

The optimization program was written using the *MATLAB Optimization Toolbox* function "fmincon", that minimizes a multivariable scalar function with restrictions. The optimization problem was stated as follows.

*At each sampling period, solve:*

$$
\min_{u_1(t+1)} J(t+1) = \left\{ \sum_{i=1}^{nu} \alpha_{1i} e_1(t+i)^2 + \alpha_{2i} e_1(t+i)^2 \right\} + \left\{ \sum_{i=1}^{nu} \lambda_{1i} \Delta u_1(t+i)^2 + \lambda_{2i} \Delta u_2(t+i)^2 \right\}
$$

where,

$$
\begin{align*}
  e_1(t) &= y_{r1}(t) - \dot{y}_{1i}(t) \\
  \Delta u_1(t) &= u_1(t) - u_1(t-1) \\
  e_2(t) &= y_{r2}(t) - \dot{y}_{2i}(t) \\
  \Delta u_2(t) &= u_2(t) - u_2(t-1)
\end{align*}
$$

Parameters $\alpha_{1i}$, $\alpha_{2i}$, $\lambda_{1i}$, $\lambda_{2i}$ must be tuned carefully to weigh the importance of each term. In fact this is a key subject in the problem. Selecting it heuristically, by "trial and error" procedures based on simulations results, can be long, annoying or even impossible. In this work we propose a fuzzy "self-tuning" of these parameters (called "weights").

**Fuzzy Weight Tuner.**

The Fuzzy Inference System (FIS) are Takagi-Sugeno Zero Order, PI-like type. In fact four tables were used to determine values for $\alpha_{1i}$, $\alpha_{2i}$, $\lambda_{1i}$, $\lambda_{2i}$. Fuzzy input variables are $e_1$, $e_2$, $\Delta u_1$ and $\Delta u_2$. An IF-THEN type fuzzy rule example is shown next:

"**IF** $E1(i)$ is BB and $E2(i)$ is ZZ **THEN** $\ddot{A}_{1i} = 0$, $\ddot{A}_{2i} = 4$"
The main optimization requirement that has been considered was trying to balance the influence of each term on the cost functional $J$. In Tab. 1, conclusion values $\tilde{A}_{1i}$ and $\tilde{A}_{2i}$ are shown for fuzzy rules whose input variables $e_1(i)$ and $e_2(i)$.

**Tab. 1. Look-up table for fuzzy rules.**

<table>
<thead>
<tr>
<th>$\tilde{A}<em>{1i} / \tilde{A}</em>{2i}$</th>
<th>E1SB(i)</th>
<th>E1SS(i)</th>
<th>E1ZZ(i)</th>
<th>E1BS(i)</th>
<th>E1BB(i)</th>
</tr>
</thead>
<tbody>
<tr>
<td>E2SB(i)</td>
<td>0/0</td>
<td>0/1</td>
<td>0/2</td>
<td>0/3</td>
<td>0/4</td>
</tr>
<tr>
<td>E2SS(i)</td>
<td>1/0</td>
<td>0/0</td>
<td>0/1</td>
<td>0/2</td>
<td>0/3</td>
</tr>
<tr>
<td>E2ZZ(i)</td>
<td>2/0</td>
<td>1/0</td>
<td>0/0</td>
<td>0/1</td>
<td>0/2</td>
</tr>
<tr>
<td>E2BS(i)</td>
<td>3/0</td>
<td>2/0</td>
<td>1/0</td>
<td>0/0</td>
<td>0/1</td>
</tr>
<tr>
<td>E2BB(i)</td>
<td>4/0</td>
<td>3/0</td>
<td>2/0</td>
<td>1/0</td>
<td>0/0</td>
</tr>
</tbody>
</table>

**SIMULATION RESULTS**

In Fig.5 and Fig.6 results of an open loop simulation for $C_b$ (mol/l) and $T(°C)$, with perturbation steps in $T_0$, are shown.

**Fig.5.** $C_b$(mol/lts) open-loop.

**Fig.6.** $T(°C)$ open-loop.

**Fig.7.** $C_b$(mol/lts) closed-loop.

**Fig.8.** $C_b$(mol/lts) closed-loop.
In order to show the controller performance, step perturbations were simulated in temperature $T_0$ in closed-loop mode. Fig.7 and Fig.8 show results of this simulation.

CONCLUSIONS
Designers have to cope with many practical problems when trying to use advanced control techniques. In fact, the main idea behind this work was to develop a method for weights self-tuning in order to ease the controller design. The proposed method shows good results and has a major advantage because of its simplicity. Simulations were carried in a standard PC Intel Celeron 766Mhz using MATLAB version 6.0. It was found that with 3000 iterations (≈2hours), dependent on fuzzy look-up tables values, parameter vectors were well tuned, better than all values calculated by "trial and error". The method could be easily implemented with standard industrial controllers. However, improvements in fuzzy rules could be achieved by using more powerful techniques for optimizing conclusions and fuzzy variable membership.

REFERENCES